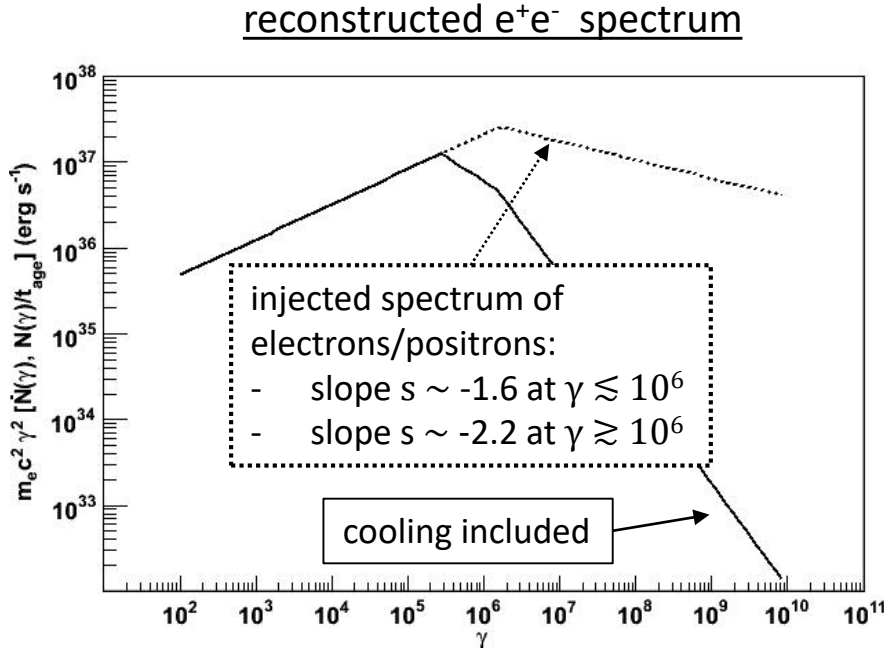
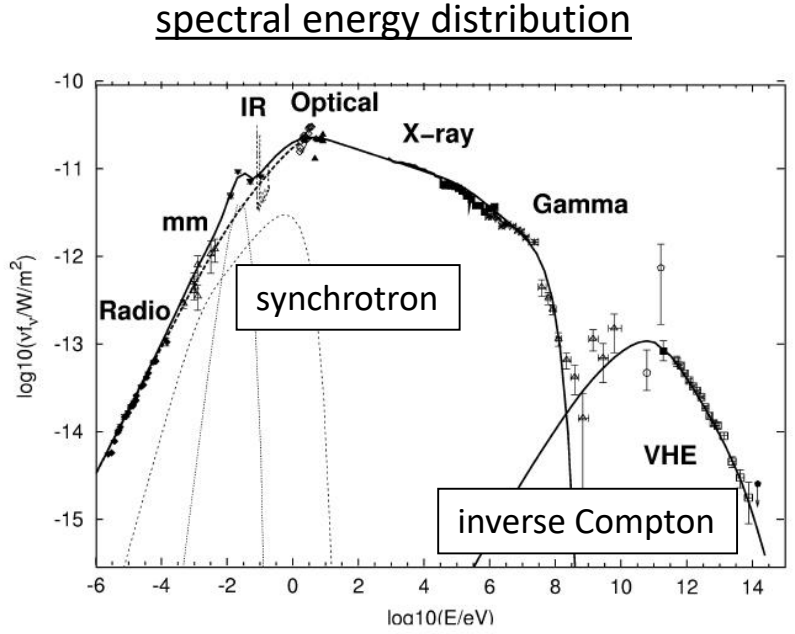
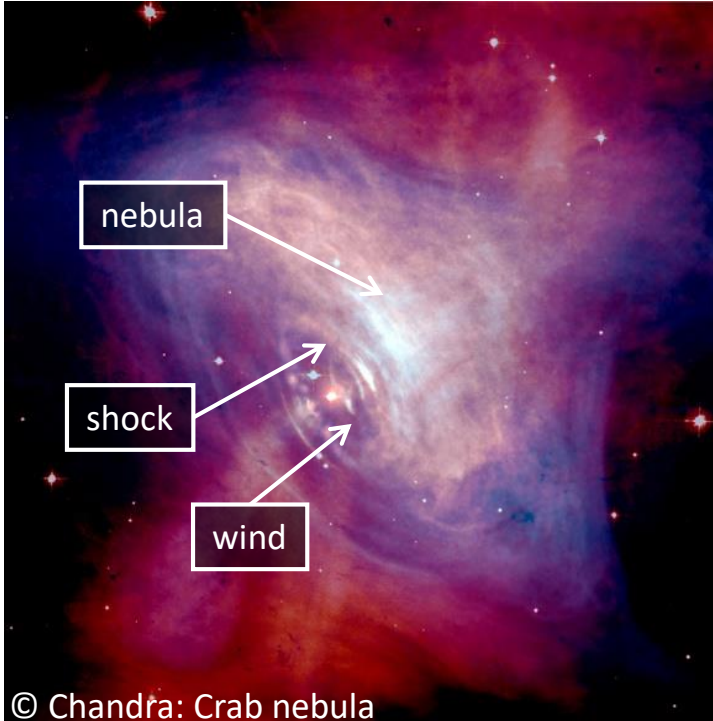


Recent developments on particle acceleration in magnetized turbulence

1. Comisso, L., & Sironi, L. : The Interplay of Magnetically Dominated Turbulence and Magnetic Reconnection in Producing Nonthermal Particles, *ApJ*, 886, 122 (2019).
 2. Comisso, L., & Sironi, L. : Particle Acceleration in Relativistic Plasma Turbulence, *PRL*, 121, 255101 (2018).
 3. Zhdankin, V. : Particle energization in relativistic plasma turbulence: solenoidal versus compressive driving, arXiv e-prints, arXiv:2106.00743 (2021).
 4. Zhdankin, V., Uzdensky, D. A., Werner, G. R., & Begelman, M. C. : Electron and Ion Energization in Relativistic Plasma Turbulence, *PRL*, 122, 055101 (2019).
 5. Zhdankin, V., Uzdensky, D. A., Werner, G. R., & Begelman, M. C. : System-size Convergence of Nonthermal Particle Acceleration in Relativistic Plasma Turbulence, *ApJ*, 867, L18 (2018).
 6. Zhdankin, V., Werner, G. R., Uzdensky, D. A., & Begelman, M. C. : Kinetic Turbulence in Relativistic Plasma: From Thermal Bath to Nonthermal Continuum, *PRL*, 118, 055103 (2017).
 7. Wong, K., Zhdankin, V., Uzdensky, D. A., Werner, G. R., & Begelman, M. C.: First-principles Demonstration of Diffusive-advective Particle Acceleration in Kinetic Simulations of Relativistic Plasma Turbulence, *ApJ*, 893, L7 (2020).
- + Lemoine, M., Malkov, M. A.: Powerlaw spectra from stochastic acceleration, *MNRAS*, 499, 4972 (2020).
Lemoine, M.: Particle acceleration in strong MHD turbulence, arXiv:2104.08199 (2021).

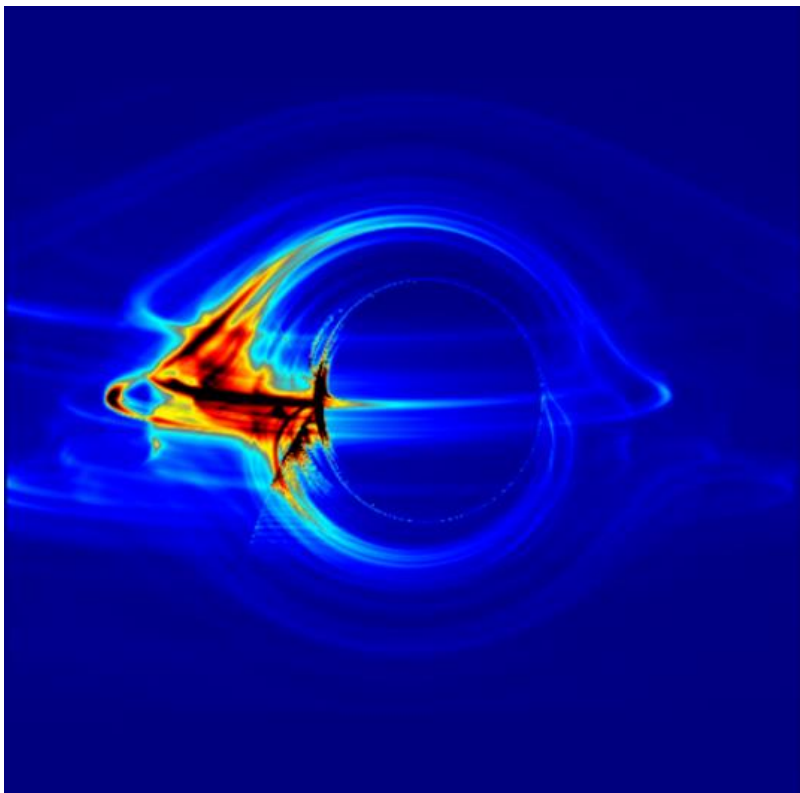
Pulsar wind nebulae as extreme lepton accelerators...



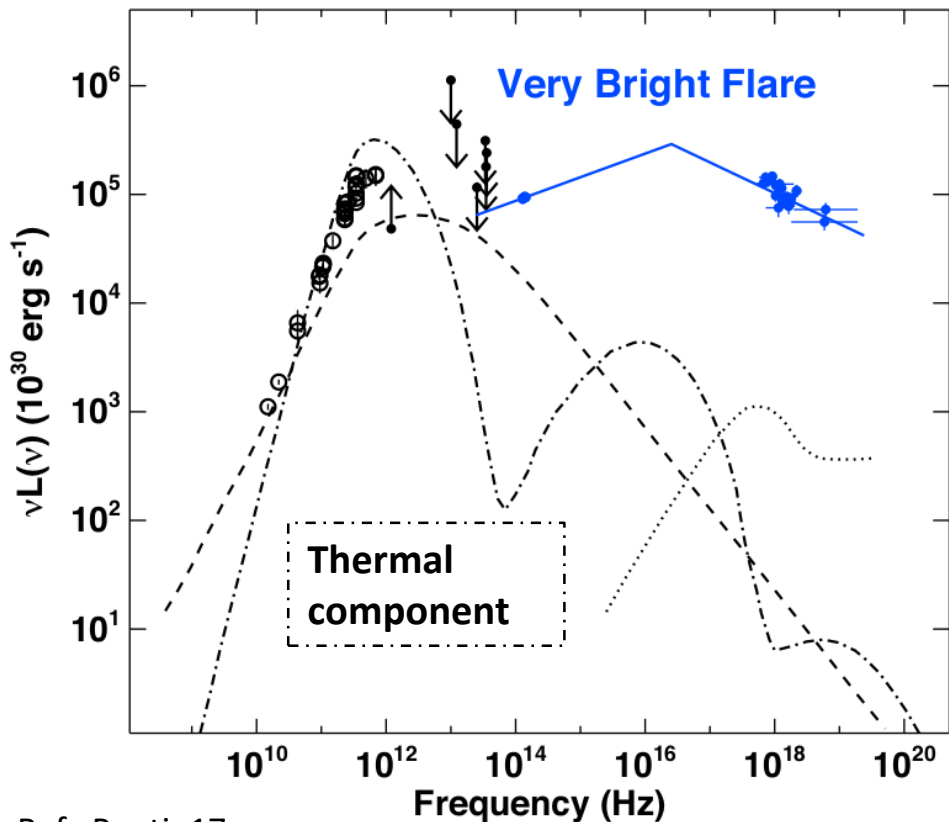
→ in the nebula: magnetization $\sigma = \frac{u_{magnetic}}{u_{plasma}} \sim 1$ (relativistic turbulence!),
 ... composition pair plasma, $\ell_c \sim 0.1 \text{ pc}$, $\frac{c}{\omega_p} \sim 10^{-6} \text{ pc}$

Evidence for non-thermal electron acceleration in BH environments...

→ Flares seen in NIR and X around SgrA*: suggest powerlaw extension with slope ~ -3 , + synchrotron cooling break...
⇒ key scenarios: reconnection (at large magnetization), or turbulence (if large fluctuations)?



Ref.: Petersen+Gammie20



Ref.: Ponti+17

NB: as in many astrophysical sources, a huge hierarchy between macroscopic scales (l_c turbulence scale, r_g) and microscopic scales (r_L): $r_g/r_L \sim 10^6$ for a GeV electron in 1G field... a challenge for numerical simulations!

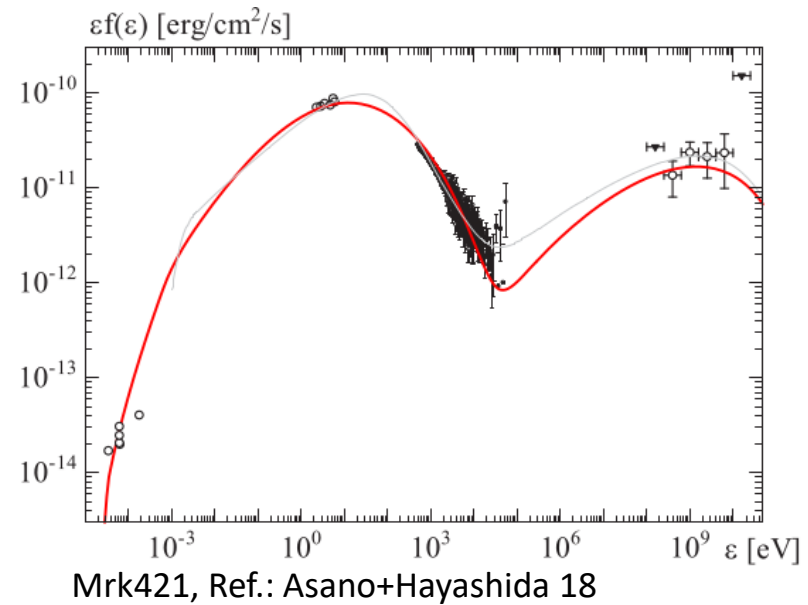
Non-thermal electrons in jets... on all scales!

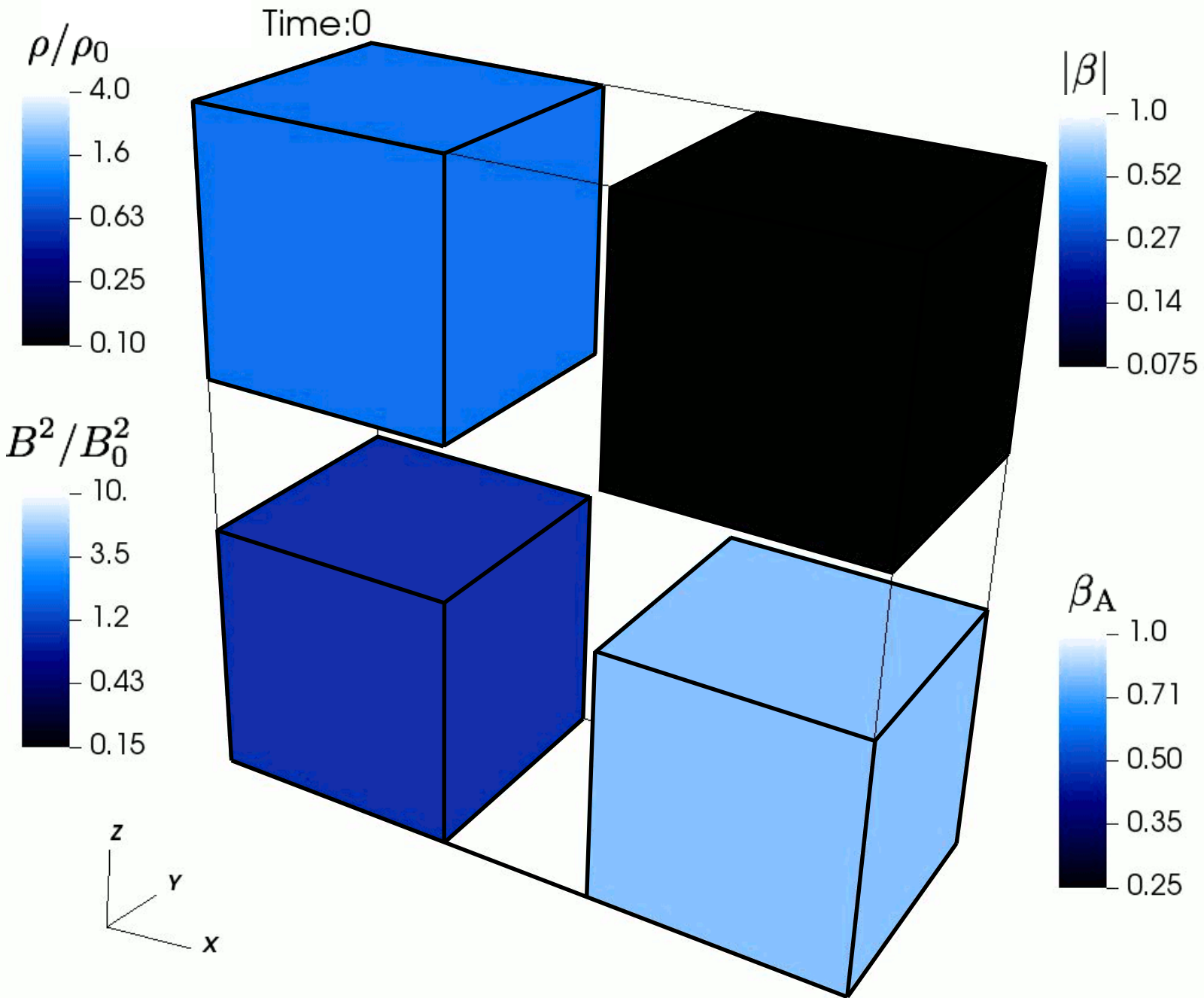


© Chandra: X-ray jet from Cen A

→ in large-scale jets:
radiation in X-ray over length scales \gg synchrotron cooling length requires some continuous acceleration, with index $\sim -2 \dots -3$, e.g. turbulence or shear?
Refs.: Liu+17, Rieger 19

→ in blazars:
generic SSC or synchrotron+EC model from non-thermal electrons... acceleration physics: reconnection, turbulence, shocks?
e.g. for turbulence:





Relativistic MHD simulation (256^3 , $\sigma_0=30$, $u_A \sim 5$) © C. Demidem

Turbulence characteristics:

→ energy injection scale: ℓ_c

→ magnetization: $\sigma = \frac{u_{\text{magnetic}}}{u_{\text{plasma}}}$

→ Alfvén 4-velocity: $u_A = \sqrt{\sigma}$

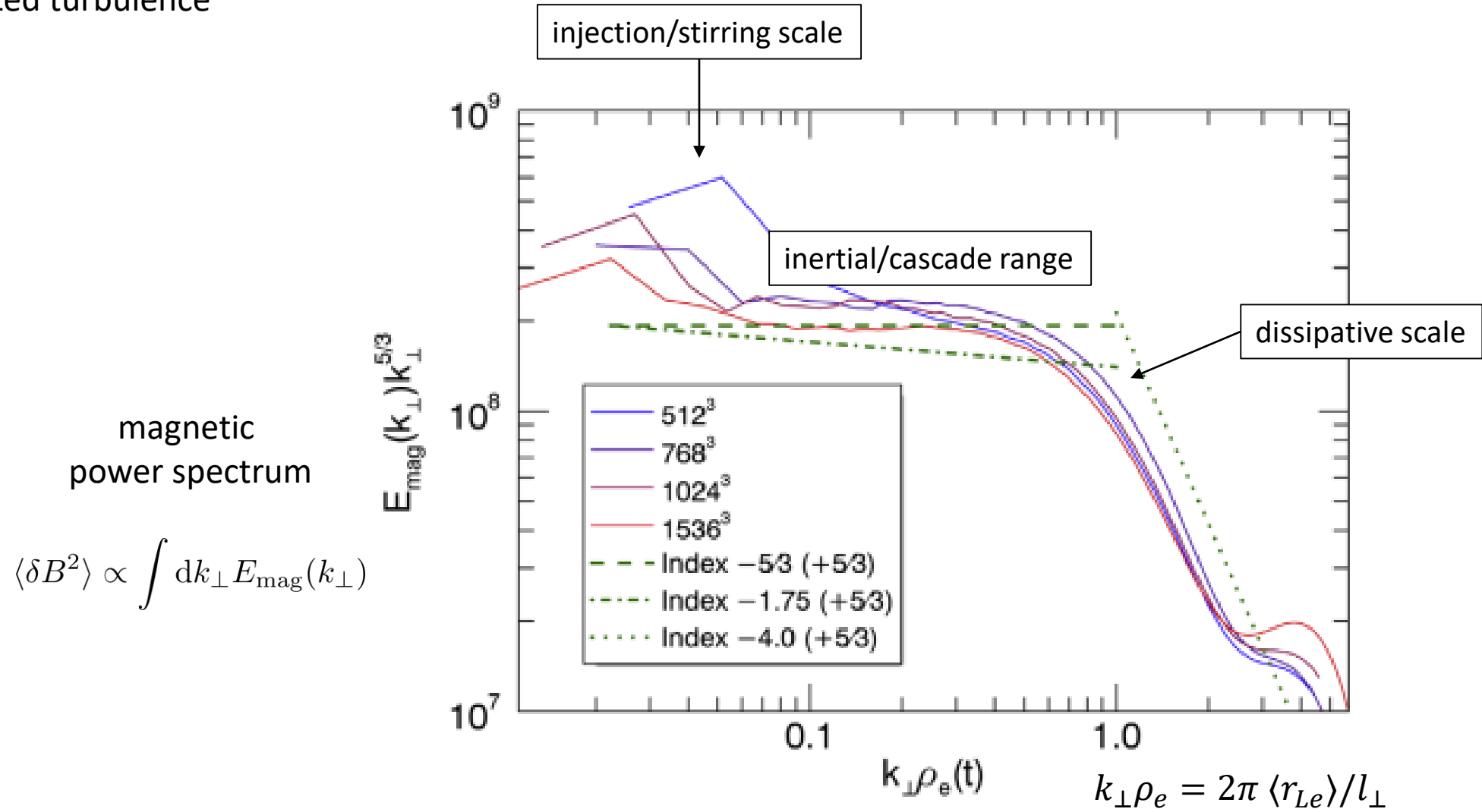
⇒ relativistic turbulence: $\sigma > 1$

→ dissipation scales: at plasma Larmor or skin depth scale c/ω_p

⇒ dynamic range in PIC:

$$\frac{\ell_c}{c/\omega_p} \sim \mathcal{O}(100)$$

... using PIC (~ electromagnetic N-body code) to perform self-consistent, ab initio virtual experiments of relativistic magnetized turbulence



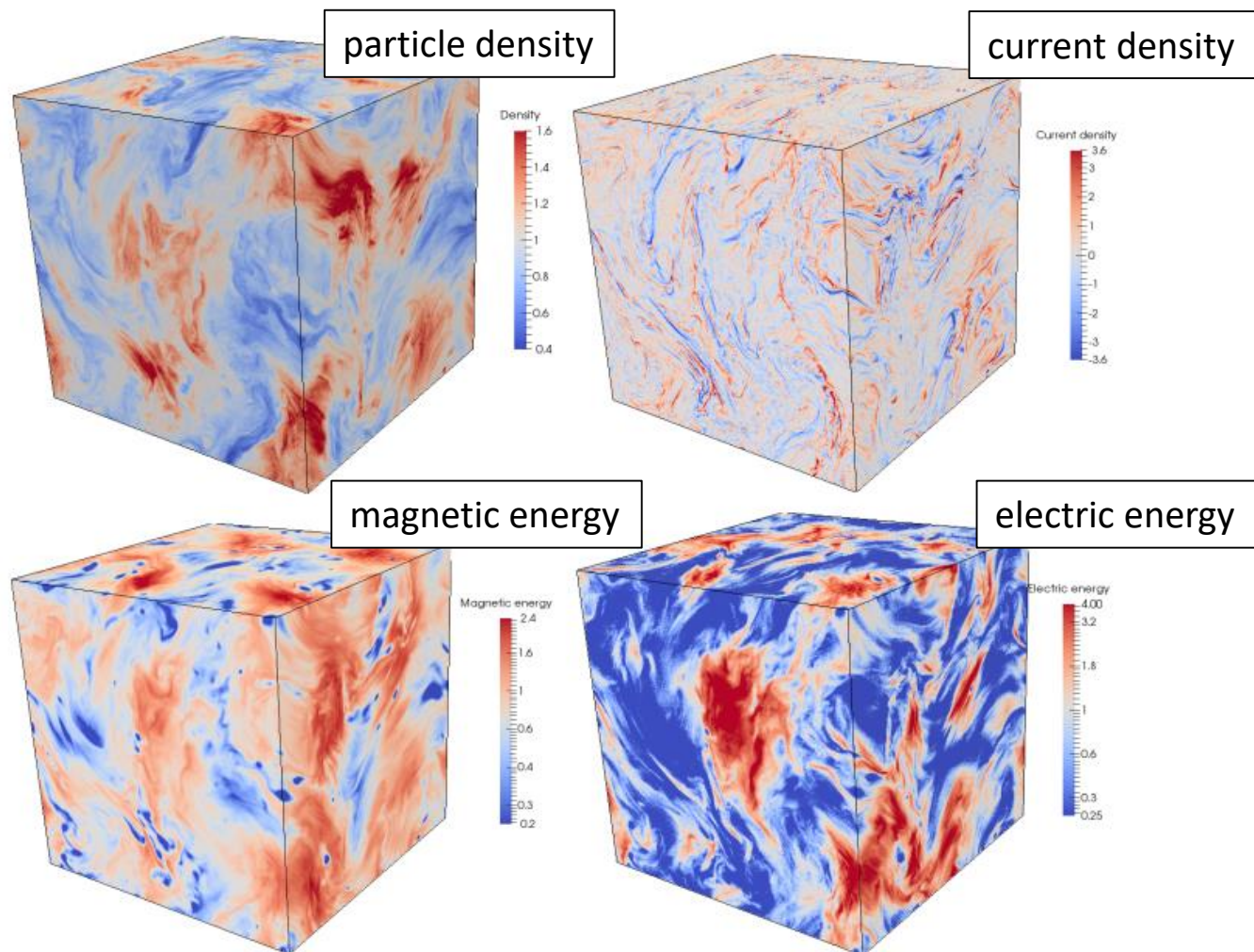
inertial range: MHD-type turbulent cascade

kinetic scales: dissipative processes (reconnection)

+ self-consistent particle-turbulence interaction → particle acceleration

Table 1. List of largest simulations

Case	N^3	$L/2\pi\rho_{c0}$	σ_0	Tc/L	N_{ppc}	$R_{err,T}(\%)$	$R_{err,L/c}(\%)$
A2	1024^3	108.6	0.5	22.3	128	3.7%	0.16%
A4	1024^3	108.6	2	13.4	192	3.0%	0.23%
B1	768^3	61.1	0.25	22.3	256	3.7%	0.16%
B2	768^3	81.5	0.5	10.1	256	0.6%	0.06%
B3	768^3	81.5	1	11.2	128	2.3%	0.21%
B4	768^3	81.5	2	9.2	128	3.3%	0.36%
B5	768^3	81.5	4	13.4	96	2.4%	0.18%
C1	512^3	40.7	0.25	22.3	256	2.3%	0.10%
C2	512^3	54.3	0.5	17.9	128	0.8%	0.05%
C3	512^3	54.3	1	14.1	128	2.0%	0.14%
C4	512^3	54.3	2	15.1	128	2.6%	0.17%
C5	512^3	54.3	4	15.6	128	2.5%	0.16%



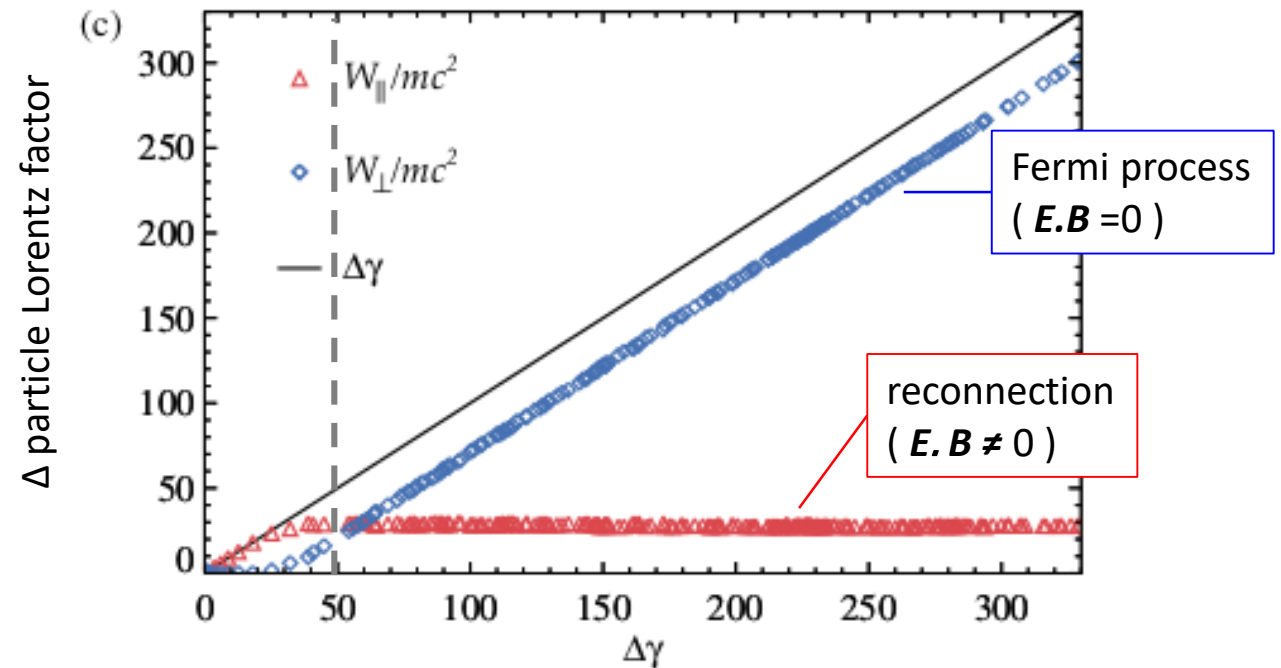
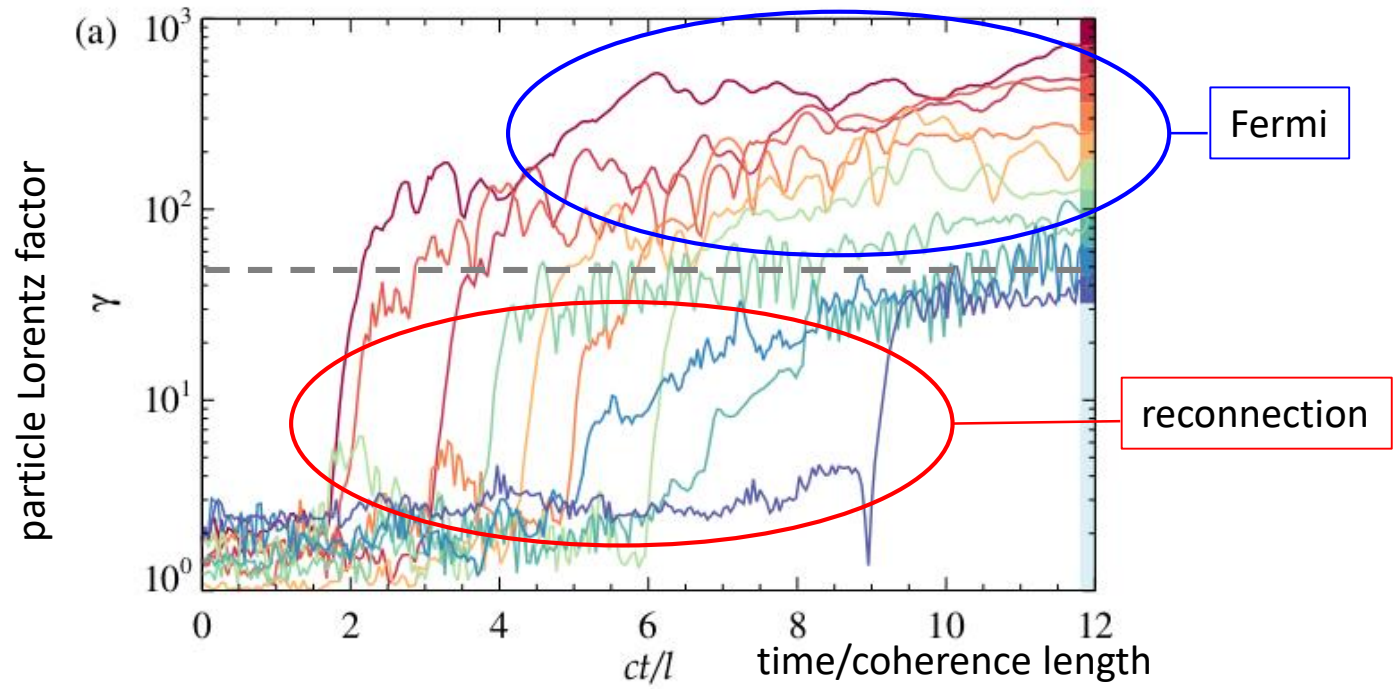
A two-stage acceleration process:

- initially, plasma is thermal: $\langle \gamma_0 \rangle \sim 3$

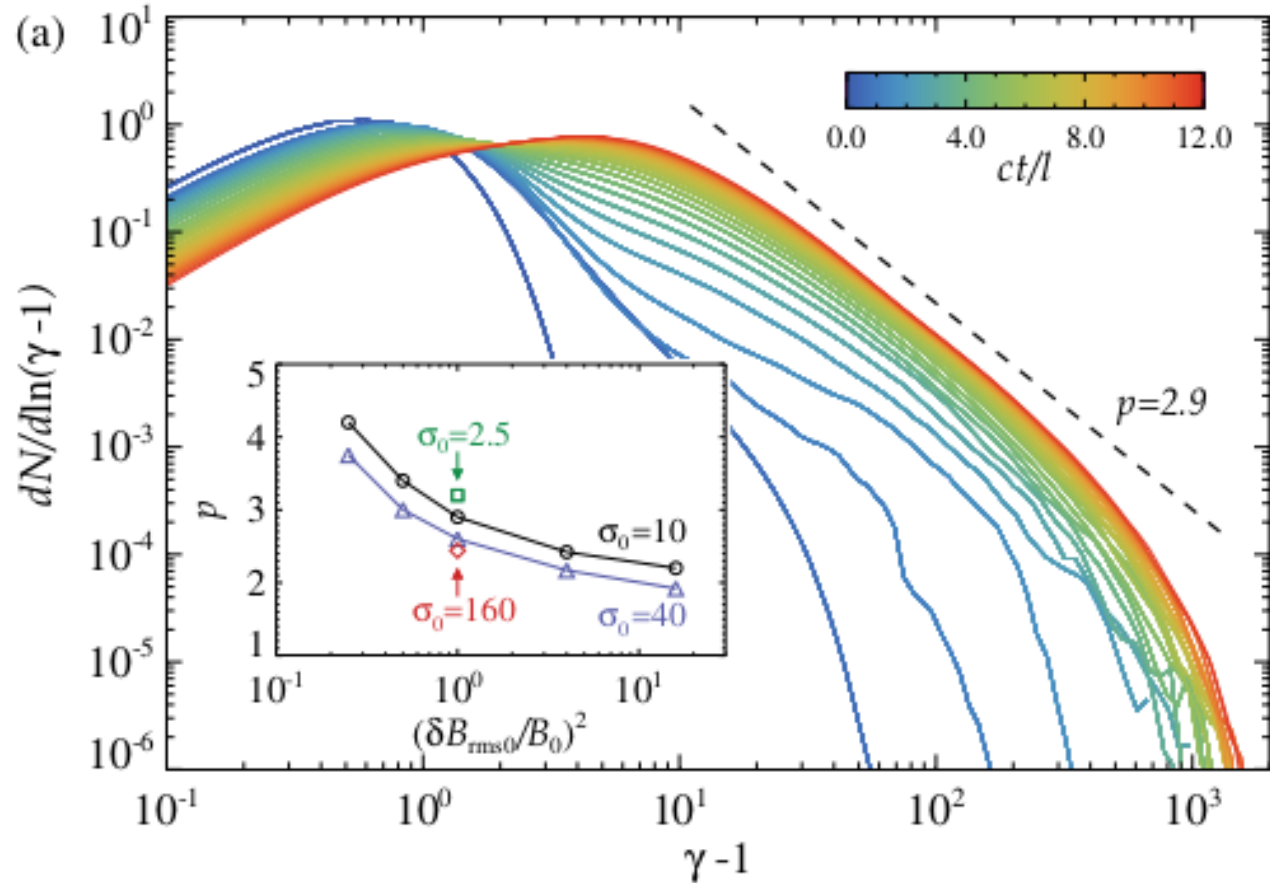
[gyroradius \sim skin depth at $\sigma \sim 0(1)$]

- first stage: particles are accelerated to $\langle \gamma \rangle \sim 4\sigma \langle \gamma_0 \rangle$ in reconnection layers (dissipative physics on kinetic scales)

- second stage: particles are accelerated to larger energies through Fermi-type (stochastic Fermi acceleration) processes...

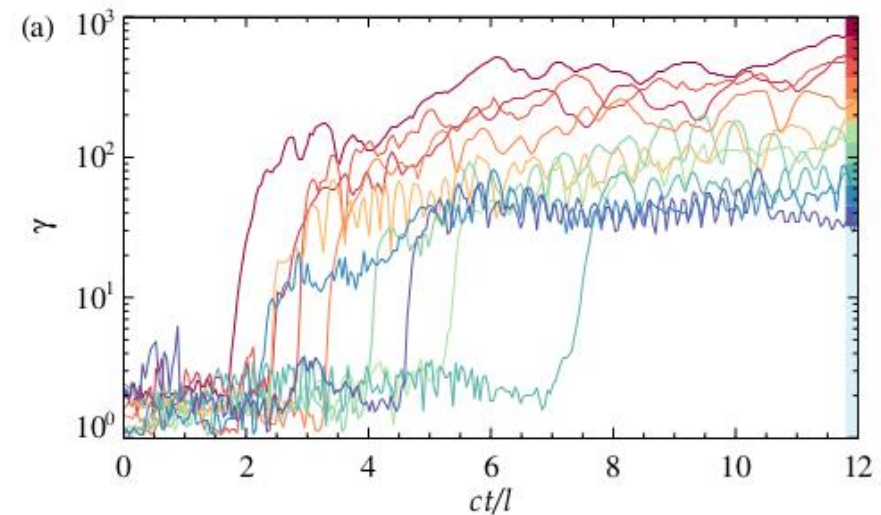


Generation of a non-thermal powerlaw spectrum

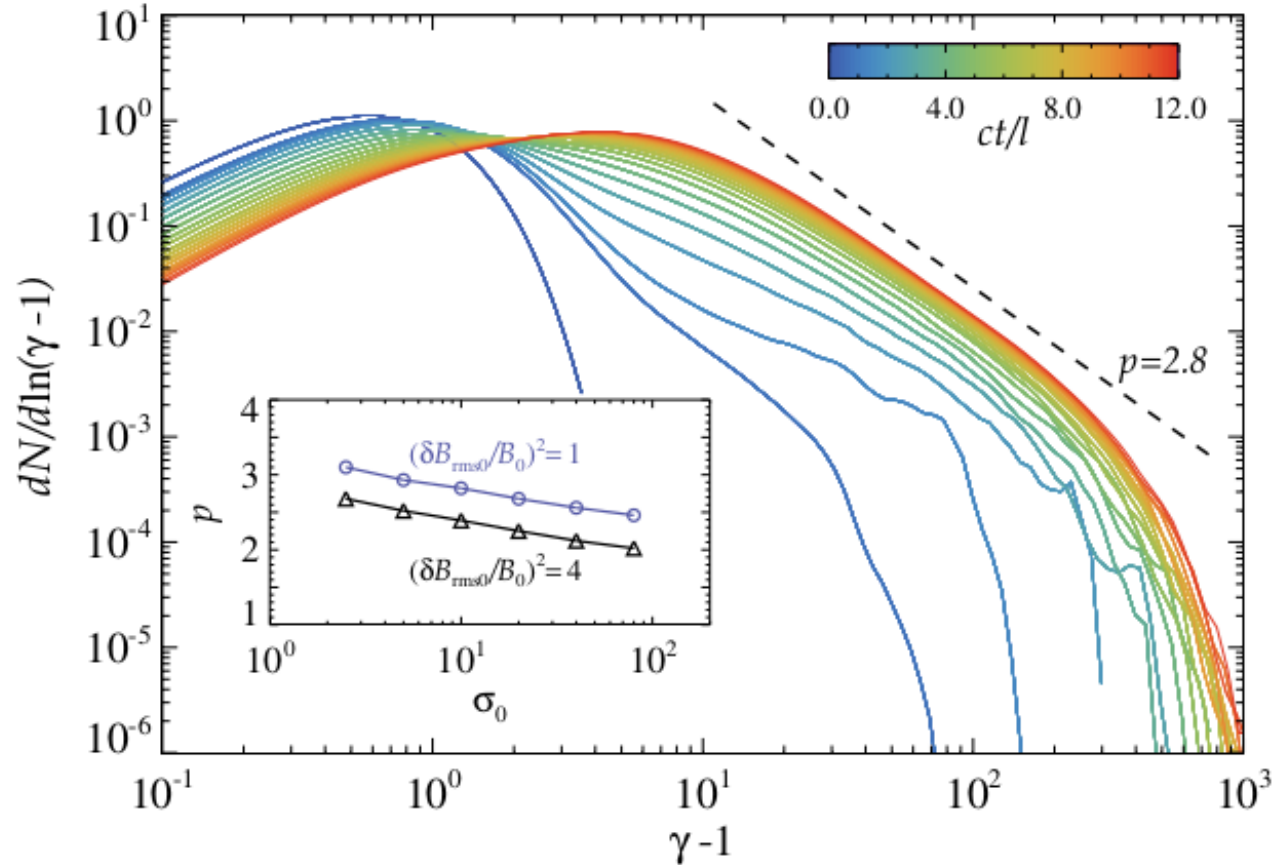


- a thermal core, heating through dissipative processes at kinetic scales (reconnection)...

- a non-thermal (soft) powerlaw tail from Fermi acceleration



Generation of a non-thermal powerlaw spectrum



- a thermal core, heating through dissipative processes at kinetic scales (reconnection)...

- a non-thermal (soft) powerlaw tail from Fermi acceleration

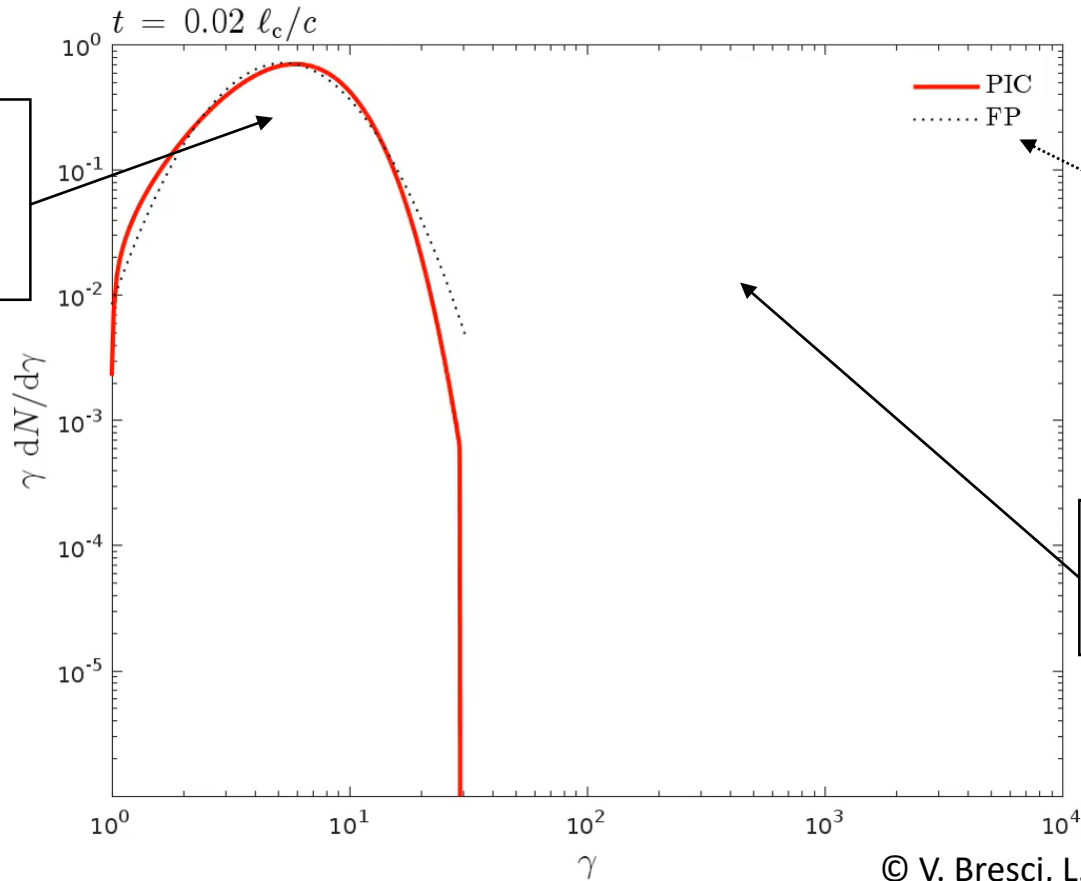
- tendency: spectrum becomes harder with increasing magnetization (= increasing v_A/c), with increasing amplitude $(\delta B/B)$...

Measured momentum diffusion coefficient (in supra-thermal tail):

$$D_{pp} \sim 0.1 \langle \delta u^2 \rangle \frac{p^2}{\ell_c/c}$$

→ a powerlaw spectra from Fermi acceleration in a closed box?

PIC simulations invalidate the Fokker-Planck description of stochastic acceleration¹



QLT/Fokker-Planck prediction:

$$\text{FP: } \frac{\partial}{\partial t} f(p, t) = \frac{1}{p^2} \frac{\partial}{\partial p} \left[p^2 D_{pp} \frac{\partial}{\partial p} f(p, t) \right]$$

$$\Rightarrow \text{sol.: } p^3 f(p, t) \propto \exp \left[-\frac{(\ln p - \frac{3}{2}t/t_{\text{acc}})^2}{2t/t_{\text{acc}}} \right]$$

$$t_{\text{acc}} = p^2 / D_{pp}$$

injection in thermal core:
from dissipation at kinetic
(microscopic) scales, mostly
reconnection

non-thermal tail:
from Fermi-type mechanism
(no parallel E field)

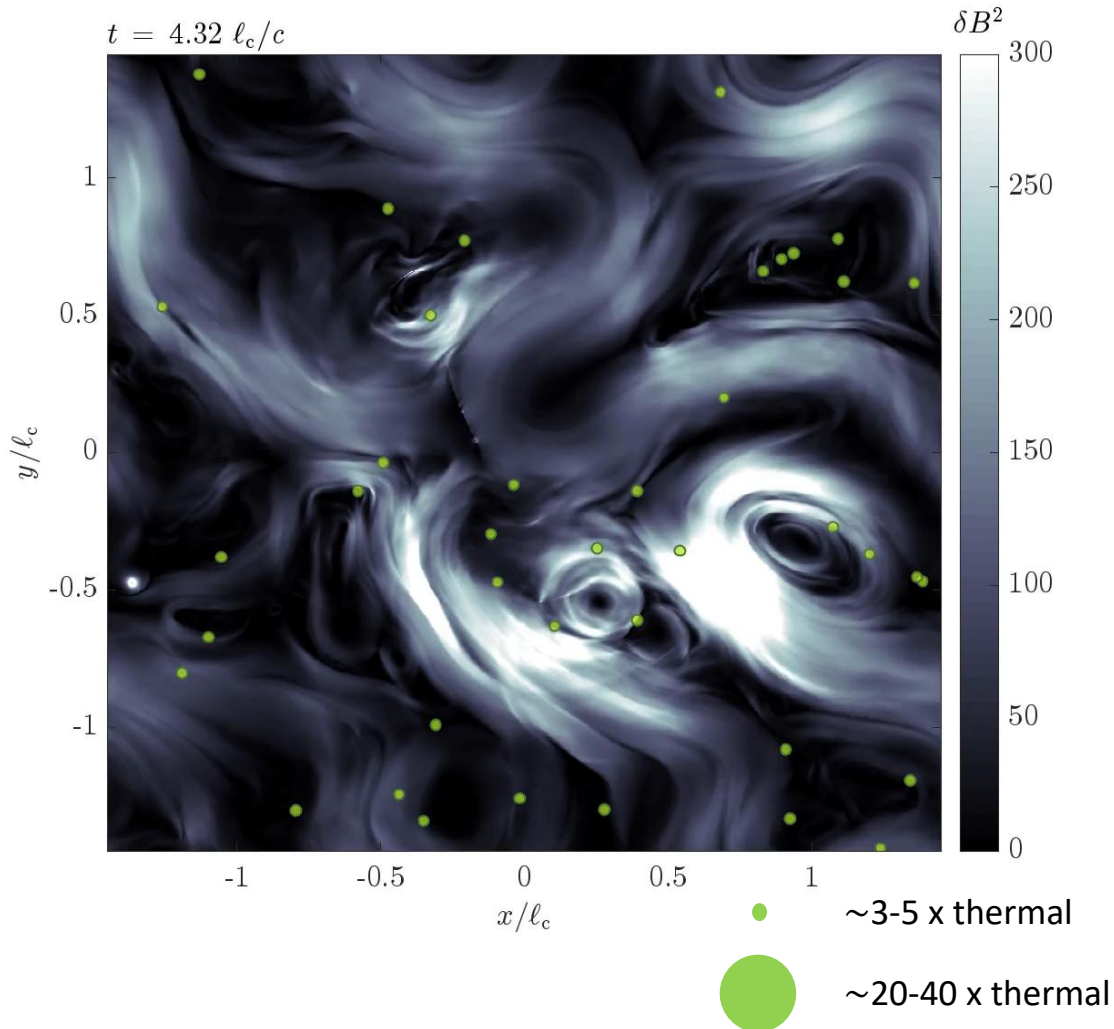
© V. Bresci, L. Gremillet, M. L.: 2D PIC, driven, e^+e^- , $10\,000^2$, $\delta B/B \sim 3$, $\sigma \sim 1$

→ consequence: Fokker-Planck is not a good model... a powerlaw tail develops, drift is slow, unlike predictions!

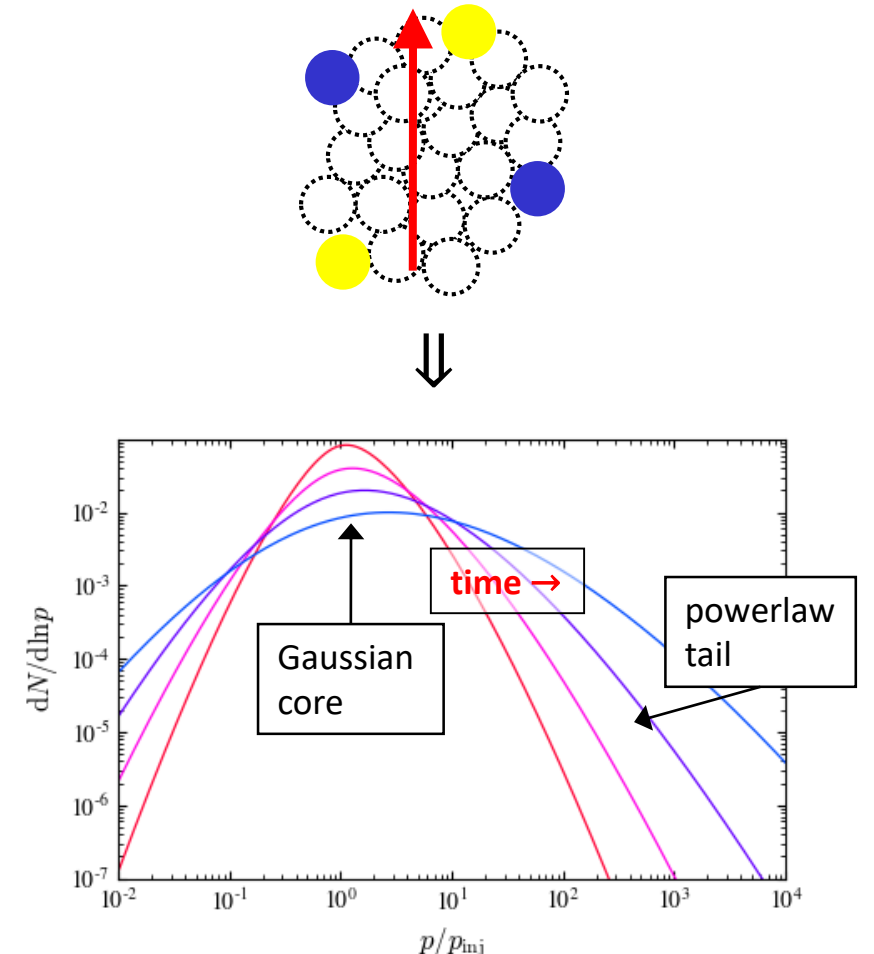
→ Interpretation²: segregation in t_{acc} among particle population...

Stochastic particle acceleration is shaped by the intermittency of the turbulence

Fokker-Planck: derives from a Langevin process with Gaussian noise, zero time coherence...
... here non-Gaussian noise, macroscopic coherence time



→ acceleration sites are localized in sparse regions, with small filling fraction, large excursions in strength



Some consequences for phenomenology and open questions

1. spectrum differs noticeably from std Fokker-Planck predictions

- no pile-up distribution, quasi-powerlaw, slow drift: impact on phenomenology?
- w/ improved model, including effects of radiative losses → recipe for inclusion in MHD/GRMHD simulations?

2. extrapolation to large hierarchy $\ell_c/(c/\omega_p)$... and other physical conditions

- quasi-powerlaw (log-running), hardening in time vs PIC sims limited in dynamic range...
- dependence on magnetization, beta-parameter, physics of stirring, composition etc.

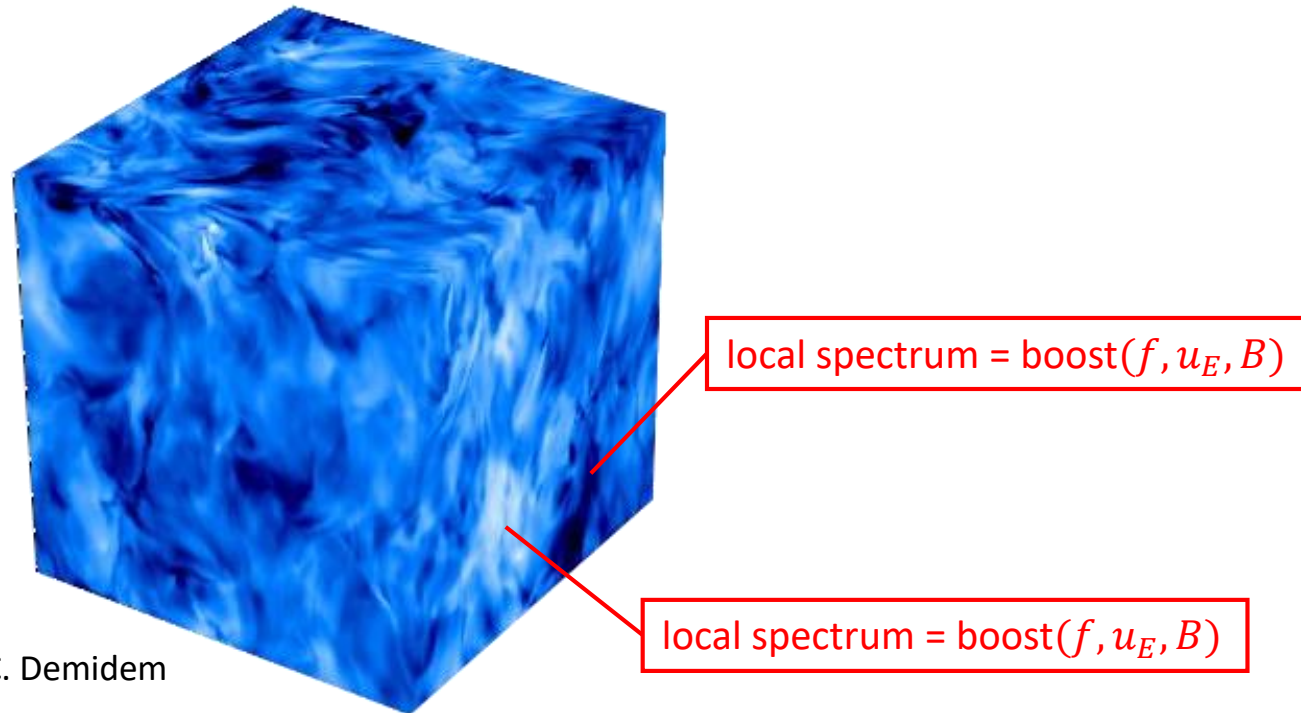
3. impact of intermittency on transport, acceleration and radiative spectra

- first experimental indication of "anomalous" transport: distribution of acceleration/scattering timescales \Rightarrow ?
- on timescale ℓ_c/c , only a small fraction of particles has scattered \Rightarrow expect anisotropies on ℓ_c scales!
- inhomogeneous particle spectra in one volume ℓ_c^3 ... consequences for flaring? (time profile?)
- inhomogeneous spectra, u_E and B in one volume ℓ_c^3 ... consequences for radiative spectra?

Some consequences for phenomenology and open questions

3. impact of intermittency on transport, acceleration and radiative spectra

- no one-to-one relation $t_{\text{acc}}(\gamma)$: distribution of acceleration/scattering timescales \Rightarrow ?
- on timescale ℓ_c/c , only a small fraction of particles has scattered \Rightarrow expect anisotropies on ℓ_c scales!
- inhomogeneous particle spectra in one volume ℓ_c^3 ... consequences for flaring? (time profile?)
- inhomogeneous spectra, u_E and B in one volume ℓ_c^3 ... consequences for radiative spectra?



e.g., Bykov+13 in connection to Crab flares, Khangulyan+21 for synchrotron in inhomogeneous B

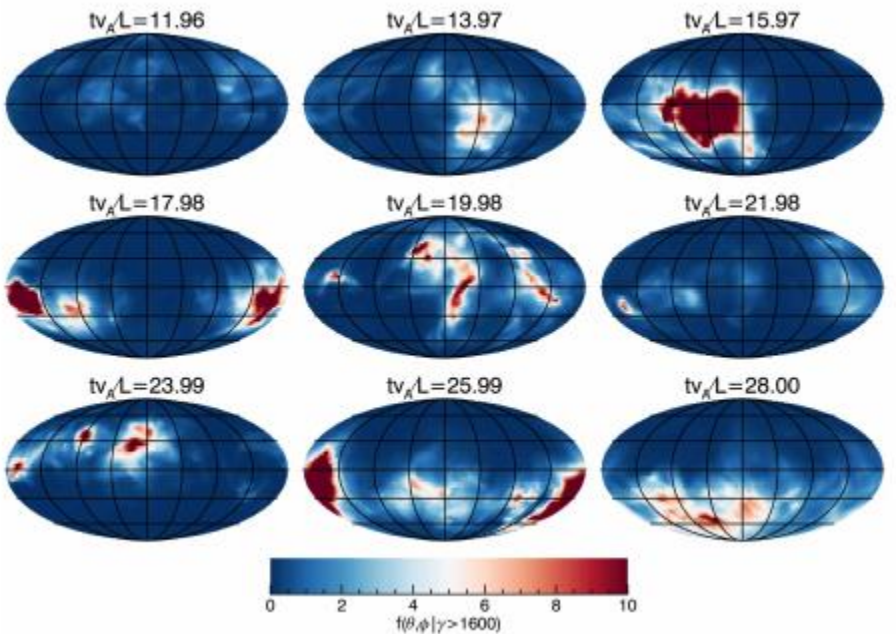
Some consequences for phenomenology and open questions

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Zhdankin+18:

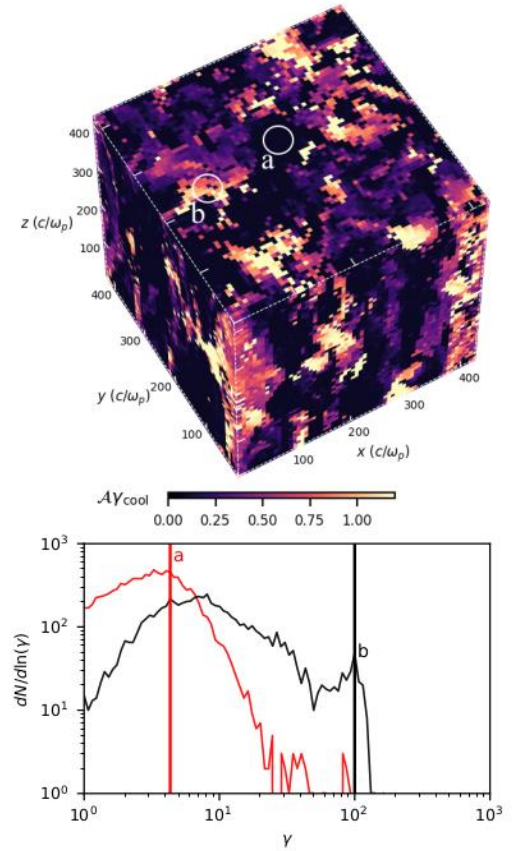
PIC, relativistic + radiative sims,



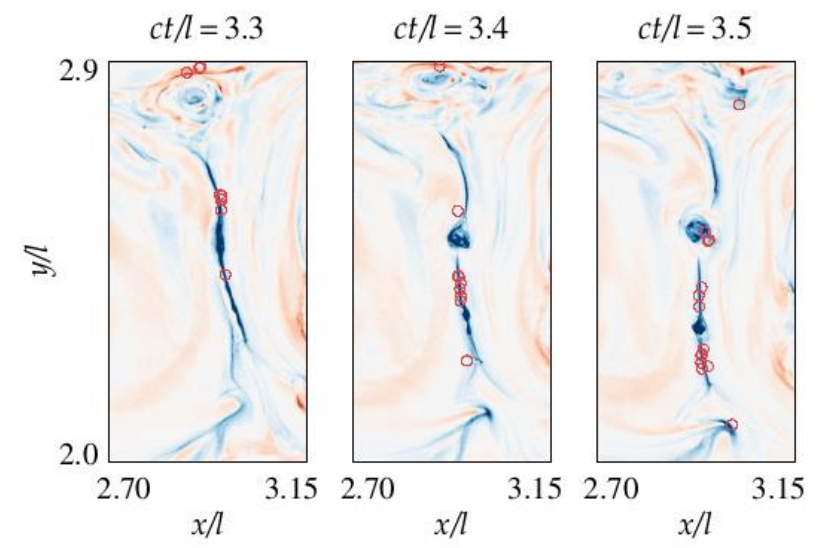
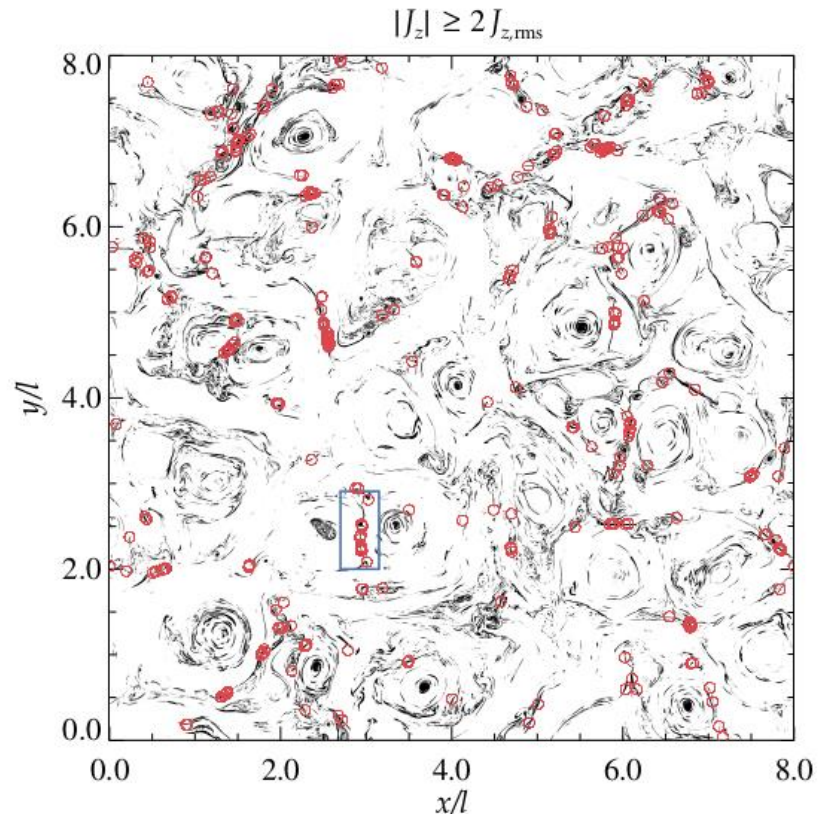
anisotropic momentum distribution at large momenta

Nättilä+Beloborodov 20:

PIC, relativistic + radiative sims,



Injection in reconnection layers



Turbulence in e-ion plasmas: differential heating

